## Fighting Multicollinearity in Double Selection: A Bayesian Approach Research practice 2: Proposal presentation

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Problem statement Context Methodology Objectives References
Intuition on what we want to do

"Many empirical analyses focus on estimating the structural, causal, or treatment effect of some variable on an outcome of interest. For example, we might be interested in estimating the causal effect of some government policy on an economic outcome such as employment.(...) A problem empirical researchers face when relying on a conditional-on-observables identification strategy for estimating a structural effect is knowing which controls to include." Belloni et al. [2013].



Consider the following structure [Belloni et al., 2013]:

$$\mathbf{y}_i = \alpha \mathbf{d}_i + \mathbf{x}_i' \beta_{\mathbf{g}} + \epsilon_i \tag{1}$$

$$d_i = x_i^{\prime} \beta_m + \zeta_i \tag{2}$$

where  $y_i$  is the response,  $\beta_g$ ,  $\beta_m$  are the structural and treatments effects of variables  $x_i$  respectively,  $d_i$  is the treatment,  $\alpha$  is the treatment effect and  $\epsilon_i$ ,  $\zeta_i$  are stochastic errors such that

$$E\left[\epsilon_{i} \mid x_{i}, d_{i}\right] = E\left[\zeta_{i} \mid x_{i}\right] = 0$$

Problem statement	Context ●00	Methodology	Objectives	References
Previous works				

Belloni et al. [2013] showed that assumptions over the distribution of  $\sqrt{n}(\alpha - \hat{\alpha})$  are not always true via simulation:

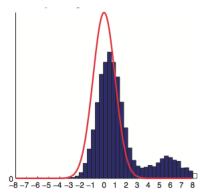


Figure: Theorical and simulated distrubution, taken from Belloni et al. [2013].

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The Lasso estimator as introduced in Tibshirani [1996] is an optimization problem which solves the following:

$$\beta^{*} = \min_{\beta \in R^{p}} \sum_{i=1}^{n} [d_{i} - x_{i}^{'}\beta_{m}]^{2} + \lambda \sum_{j=1}^{p} |\beta_{j}|$$
(3)

where  $\lambda$  is a penalization coefficient



Post double LASSO estimator is a three stages procedure:

- Proceed with LASSO estimator on the treatment effect.
- Proceed with LASSO estimator on the structural equation but without including the treatment.
- Proceed with a linear regression on the structural equation using the treatment and the union of variables that were selected on previews stages.

Problem statement	Context 000	Methodology	Objectives	References
MC <sup>3</sup>				

Markov chain Monte Carlo model composition (MC<sup>3</sup>) is a Bayesian methodology which uses a stochastic search comparing different models by its posterior model probability. As in Simmons et al. [2010], let  $M = \{M_1, M_2, ..., M_m\}$  the set of models under consideration, and d the observed data as in (2).

Problem statement	Context 000	Methodology	Objectives	References
MC <sup>3</sup>				

The posterior model probability for model  $M_j$  is defined as

$$P(M_j \mid d, M) = \frac{P(d \mid M_j)\pi(M_j)}{\sum_{i=1}^{m} P(d \mid M_i)\pi(M_i)} \quad \forall j = 1, 2, ...m$$

where  $P(d \mid M_j)$  is the integrated likelihood of the model  $M_j$  and  $\pi(M_j)$  is the prior of the prior probability that  $M_j$  is the true model.



The idea of a nonlocal (to 0) prior is to effectively eliminate models with unnecessary explanatory variables, for instance consider the following nonlocal prior proposed by Johnson and Rossell [2012]:

$$\pi(\beta \mid \tau, \ \sigma^{2}, \ r) = d_{p}(2\pi)^{-p/2}(\tau\sigma^{2})^{-rp-p/2} \mid A_{p} \mid^{1/2} exp\left\{-\frac{1}{2\tau\sigma^{2}}\beta'A_{p}\beta\right\} \prod_{i=1}^{p}\beta_{i}^{2r}$$
(4)

where  $\tau$ , r,  $A_p$  are hyper-parameters for the prior.

Problem statement	Context 000	Methodology	Objectives	References
General ob	jective			

To propose a methodology based on MC<sup>3</sup> in order to compare its performance on the inference of a treatment based on frequentist results given by the double post LASSO estimators.

Problem statement	Context 000	Methodology	Objectives	References
Specific ob	jectives			

- Implement the post double selection and MC<sup>3</sup> on simulations exercises.
- Gather real information as in Donohue III and Levitt [2001], and use both methodologies.
- Compare both methodologies and analyse how they perform based on simulation and real cases.

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References I				

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- Donohue III, J. J. and Levitt, S. D. (2001). The impact of legalized abortion on crime. *Quarterly Journal of Economics*, pages 379–420.
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Problem statement	Context 000	Methodology	Objectives	References
References II				

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Problem statement

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## Any questions?

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