TABLE 5 Boolean Identities.

| Identity | Name |
| :---: | :---: |
| $\overline{\bar{x}}=x$ | Law of the double complement |
| $\begin{aligned} & x+x=x \\ & x \cdot x=x \end{aligned}$ | Idempotent laws |
| $\begin{aligned} & x+0=x \\ & x \cdot 1=x \end{aligned}$ | Identity laws |
| $\begin{aligned} & x+1=1 \\ & x \cdot 0=0 \end{aligned}$ | Domination laws |
| $\begin{aligned} & x+y=y+x \\ & x y=y x \end{aligned}$ | Commutative laws |
| $\begin{aligned} & x+(y+z)=(x+y)+z \\ & x(y z)=(x y) x \end{aligned}$ | Associative laws |
| $\begin{aligned} & x+y z=(x+y)(x+z) \\ & x(y+z)=x y+x z \end{aligned}$ | Distributive laws |
| $\begin{aligned} & \overline{(x y)}=\bar{x}+\bar{y} \\ & (x+y)=\bar{x} \bar{y} . \end{aligned}$ | De Morgan's laws |
| $\begin{aligned} & x+x y=x \\ & x(x+y)=x \end{aligned}$ | Absorption laws |
| $x+\bar{x}=1$ | Unit property |
| $x \bar{x}=0$ | Zero property |

The reader should compare the Boolean identities in Table 5 to the logical equivalences in Table 6 of Section 1.2 and the set identities in Table 1 in Section 2.2. All are special cases of the same set of identities in a more abstract structure. Each collection of identities can be obtained by making the appropriate translations. For example, we can transform each of the identities in Table 5 into a logical equivalence by changing each Boolean variable into a propositional variable, each 0 into a $\mathbf{F}$, each 1 into a T, each Boolean sum into a disjunction, each Boolean product into a conjunction, and each complementation into a negation, as we illustrate in Example 9.

TABLE 6 Verifying One of the Distributive Laws.

| $x$ | $y$ | $z$ | $y+z$ | $x y$ | $x z$ | $x(y+z)$ | $x y+x z$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 |
| 1 | 0 | 1 | 1 | 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

